

GCSE MATHEMATICS

New Specimen Papers published June 2015

Paper 3 Higher - Mark Scheme

8300/3H

Version 1.0



Principal Examiners have prepared these mark schemes for specimen papers. These mark schemes have not, therefore, been through the normal process of standardising that would take place for live papers.

Further copies of this Mark Scheme are available from aqa.org.uk

Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

М	Method marks are awarded for a correct method which could lead to a correct answer.
Α	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
SC	Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
Mdep	A method mark dependent on a previous method mark being awarded.
Bdep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent.
	eg accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between <i>a</i> and <i>b</i> inclusive.
3.14	Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416
Use of brackets	It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.



Q	Answer	Mark	Comments
			-
1	10 000	B1	
	Γ		
2	$\begin{pmatrix} 7\\-5 \end{pmatrix}$	B1	
	- -		
3	0.667	B1	
	1		
4	D	B1	

	Alternative method 1		
	6.31 – 3.6(0) or 2.71	M1	
	their 2.71 ÷ 3.6(0) (× 100) or 0.752(7) or 0.753	M1dep	
	75.2(7) or 75.28 or 75.3	A1	Allow 75 with correct method seen
5	Alternative method 2		
	6.31 ÷ 3.6(0) (× 100) or 1.752(7) or 1.753 or 175.2(7) or 175.3	M1	
	1.752(7) – 1 or 1.753 – 1 or 175.2(7) – 100 or 175.3 – 100	M1dep	
	75.2(7) or 75.28 or 75.3	A1	Allow 75 with correct method seen

Q	Answer	Mark	Comments
	9 + $3x + x - 5 + 2x$ or $6x + 4$ or $3x + x - 5 + 2x$ or $6x - 5$	M1	oe
6	their $(6x + 4) = 100$ or their $6x - 5 = 91$ or $6x = 96$	M1	$\frac{9}{\text{their } (6x+4)} = \frac{9}{100}$
	$x = 16$ $\frac{11}{100}$	A1 B1ft	ft their 16
7	One continuous arc, centre <i>A</i> , intersecting <i>AB</i> and <i>AD</i> or Two arcs, each with same radius and centre <i>A</i> , intersecting <i>AB</i> and <i>AD</i> Intersecting arcs with same radius and centres at the intersections with <i>AB</i> and <i>AD</i> and angle bisector drawn	M1 A1	Allow \pm 2 mm for radii Allow \pm 2 mm for radii The radius of these arcs need not be the same as those used for M1
	Arc of radius [5.8, 6.2] cm, centre <i>C</i> , intersecting their angle bisector and <i>P</i> labelled $P = \frac{P}{P} = \frac{P}{P} = \frac{P}{P}$		SC1 Arc of radius [5.8, 6.2] cm, centre <i>C</i> with no angle bisector attempted



Q	Answer	Mark	Comments
8(a)	375.112(1656)	B1	Condone if correctly rounded to 7 significant figures or better eg 375.1122
9(b)	20 ² or 400 or ³ √1000 or 10 or 5	M1	
8(b)	$400 - 10 \div 5 = 398$ or 400 - 2 = 398	A1	
		1	

9	octagon	B1	
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Q	Answer	Mark	Comments
	Alternative method 1		
	$\angle PCB = 180 - 90 - 15 \text{ or } 75^{\circ}$ or $\angle PCB = 90 - 15$	M1	oe Angle may be seen on diagram
	$\angle ABC = \angle PCB = \text{their 75}$ and $\angle BCD = 180 - \text{their 75 or 105}^\circ$	M1	oe Angle may be seen on diagram
	$x = 105 - 75 = 30^{\circ}$	A1	Full method required
	Alternative method 2		
	$\angle PCB = 180 - 90 - 15 \text{ or } 75^{\circ}$ or $\angle PCB = 90 - 15$	M1	oe Angle may be seen on diagram
10	$\angle ABC = \angle PCB = \text{their 75}$ and $\angle ABP = \text{their 75} - 15 \text{ or } 60^{\circ}$ and $\angle BAC = 180 - 90 - \text{their 60}$	M1	oe Angles may be seen on diagram
	$x = \angle BAC = 30^{\circ}$	A1	Full method required
	Alternative method 3		
	$\angle PCB = 180 - 90 - 15 \text{ or } 75^{\circ}$ or $\angle PCB = 90 - 15$	M1	oe Angle may be seen on diagram
	$\angle ABC = \angle PCB = \text{their 75}$ and $\angle BAC = 180 - \text{their 75} - \text{their 75}$	M1	oe Angle may be seen on diagram
	$x = \angle BAC = 30^{\circ}$	A1	Full method required



Q	Answer	Mark	Comments
	100(%) – 14(%) or 86(%) or 1 – 0.14 or 0.86	M1	Implied by 87 139(.5)
11	101 325 × 0.86 ⁴	A1	oe eg 101 325 × 0.86 or 87 139(.5) and their 87 139(.5) × 0.86 or 74 939(.97) and their 74 939(.97) × 0.86 or 64 448(.3742) and their 64 448(.3742) × 0.86
	55 425()	A1	May be implied by 55 000 or 55 400 or 55 430 or 55 426
	55 000	B1ft	ft their answer rounded to 2sf

12(a)	Ticks 'False' and states that x could be -4	B1	oe
12(b)	True and $20n \div 2n = 10$	B1	oe
12(c)	False and <i>y</i> could be between 0 and 1	B1	oe eg False and $y = 0.5$

13	Cumulative frequency 46 should be 48	B1	oe
15	Points should be plotted at end of class intervals	B1	oe

14(a)	1536	B1	
14(b)	$2^{n+2} + 2^{n+1}$	B1	

Q	Answer	Mark	Comments
	6.5 – 2.3 or 4.2 and 5 or 85 seen	M1	
	sin 5 = $\frac{6.5 - 2.3}{AD}$ or		oe
	$\cos 85 = \frac{6.5 - 2.3}{AD}$ or	M1	
15	$\left(\frac{6.5-2.3}{\tan 5}\right)^2 + \left(6.5-4.2\right)^2$		
	$\frac{6.5-2.3}{\sin 5}$ or $\frac{6.5-2.3}{\cos 85}$ or	M1dep	oe
	$\sqrt{\left(\frac{6.5-2.3}{tan5} ight)^2+\left(6.5-4.2 ight)^2}$		
	[48, 48.2]	A1	



Q	Answer	Mark	Comments	
	Alternative method 1			
	$\frac{5}{6+5+7} \text{ or } \frac{5}{18}$ or $\frac{7}{9+7+8}$ or $\frac{7}{24}$	M1	oe fraction, decimal or percentage	
	Attempt to convert to any common denominator eg $\frac{20}{72}$ and $\frac{21}{72}$ or to decimals eg 0.27(7) and 0.29 eg 3 0.28 and 0.29) or to percentages eg 28% and 29%	M1	Attempt to convert both to comparable form with one correct oe	
	$\frac{20}{72}$ and $\frac{21}{72}$ and Yes	A1	oe fractions, decimals or percentages	
16	Alternative method 2			
	Chooses a number of counters that is a multiple of 18 and 24 eg 72	M1		
	$5 imes rac{ ext{their 72}}{18}$ or 20 or $7 imes rac{ ext{their 72}}{24}$ or 21	M1		
	20 and 21 and Yes	A1		
	Alternative method 3			
	35 : 42 : 49 and 35 : 45 : 40	M1		
	$\begin{array}{c c} \frac{35}{35 + \text{their } 42 + \text{their } 49} & \text{or} & \frac{35}{126} \\ \text{or} & \\ \frac{35}{35 + \text{their } 45 + \text{their } 40} & \text{or} & \frac{35}{120} \end{array}$	M1		
	$\frac{35}{126}$ and $\frac{35}{120}$ and Yes	A1		

Q	Answer	Mark	Comments
17	(3x + a)(x + b) where $ab = 8$ or $a + 3b = 14$ or 3x (x + 4) + 2(x + 4) or x(3x + 2) + 4(3x + 2)	M1	
	(3x+2)(x+4)	A1	oe

	16×2 or 32 or $7 \times x$ or $7x$ or 20×12 or 240 or 10×17 or 170 or 16 + x + 20 + 10 or $46 + x$	M1	oe
18	$16 \times 2 + 7 \times x + 20 \times 12 + 10 \times 17$ or $16 \times 2 + 7x + 240 + 170 \text{ or}$ 442 + 7x their (32 + 7x + 240 + 170) = 8.5 × their (16 + x + 20 + 10) or their (442 + 7x) = 8.5 × their (46 + x)	M1 M1	oe Must be the sum of 4 products Award if correct expression seen, even if in an incorrect equation oe equation ft their sum of at least 3 products, one of which must be $7 \times x$ ft sum of at least 3 frequencies, one of which must be x
	their 442 – their (8.5 × 46) = 8.5 x – 7 x	M1dep	oe equation dep on 3 rd M1 Expands and rearranges their equation Allow one sign or expansion error
	34	A1	Answer 34 with no incorrect working gains 5 marks



Q	Answer	Mark	Comments
	$x^2 + 6$ or $(x - 3)^2$	M1	
	$x^2 - 3x - 3x + 9$	M1	4 terms with 3 correct
19	6 <i>x</i> < 3	M1dep	oe linear inequality dep on two quadratic expressions ft their quadratic expressions
	<i>x</i> < 0.5	A1	oe

	$\frac{\sin y}{16} = \frac{\sin 34}{10}$	M1	oe
20	$\frac{\sin 34}{10}$ × 16 or [63.47, 63.5]	M1	
	[116.5, 116.53]	A1	

Q	Answer	Mark	Comments		
	Alternative method 1				
	27.5 or 26.5 or 20.5 or 19.5 or 15.5 or 14.5 or 14.35 or 14.25 or 19.25 or 19.15 or 1.55 or 1.45	B1	Any one seen		
	a bound of 27 ÷ a bound of 1.5	M1	Must see the calculation written down 26.5 \leq a bound of 27 \leq 27.5 but not 27 1.45 \leq a bound of 1.5 \leq 1.55 but not 1.5 eg 1 27.49 \div 1.45 eg 2 26.45 \div 1.54999		
	26.5 ÷ 1.55	M1	Must see the calculation written down 26.5 ÷ 1.55 scores B1 M1 M1		
21	[17.0, 17.1]	A1	Must see method		
	Alternative method 2				
	27.5 or 26.5 or 20.5 or 19.5 or 15.5 or 14.5 or 14.35 or 14.25 or 19.25 or 19.15 or 1.55 or 1.45	B1	Any one seen		
	$17 \times a$ bound of 1.5	M1	Must see the calculation written down $1.45 \le a$ bound of $1.5 \le 1.55$ but not 1.5 eg 1 17 × 1.45 eg 2 17 × 1.54999		
	17 × 1.55	M1	Must see the calculation written down 17×1.55 scores B1 M1 M1		
	26.35 and 26.5	A1	Must see method		

Alternative method 3 on next page



Q	Answer	Mark	Comments
	Alternative method 3		
	27.5 or 26.5 or 20.5 or 19.5 or 15.5 or 14.5 or 14.35 or 14.25 or 19.25 or 19.15 or 1.55 or 1.45	B1	Any one seen
21	a bound of 27 ÷ 17	M1	Must see the calculation written down 26.5 \leq a bound of 27 \leq 27.5 but not 27 eg 1 27.49 \div 17 eg 2 26.45 \div 17
	26.5 ÷ 17	M1	Must see the calculation written down 26.5 ÷ 17 scores B1 M1 M1
	[1.558, 1.559] and 1.55	A1	

	$\frac{9}{27}$ or $\frac{18}{27}$ or fraction with denominator 22	M1	oe
22	$\frac{9}{27} \times \frac{8}{22} \text{ or } \frac{72}{594} \text{ or}$ $\frac{18}{27} \times \frac{7}{22} \text{ or } \frac{126}{594}$	M1	oe
	their $\frac{72}{594}$ + their $\frac{126}{594}$ or $\frac{198}{594}$	M1dep	oe dep on 2nd M1
	Clear indication that $\frac{198}{594}$ and $\frac{9}{27}$ are equivalent fractions	A1	

23(a)	С	B1	
22/h)	Draws tangent at $t = 3$	M1	
23(b)	[3.6, 4.4]	A1	SC1 correct gradient for their tangent

Q	Answer	Mark	Comments
	0.5 × 20 × 8 or 80 or 30 × 8 or 240 or 0.5 × (50 + 30) × 8 or 320	M1	oe Attempt at any part of the area below the graph up to 50s
24	$0.5 \times (8+5) \times 14$ or 91	M1	oe Attempt at area below the graph for time between 50s and 64s
	their 80 + their 240 + their 91 or their 320 + their 91 or 411	M1dep	dep on M1 M1 An attempt at total area for 64 seconds
	411 and Amina	A1	

25(a)	$\overrightarrow{BC} = 2\mathbf{a} - 3\mathbf{b} \text{ or}$ $\overrightarrow{CB} = -2\mathbf{a} + 3\mathbf{b} \text{ or}$ $\overrightarrow{AM} = \mathbf{a} \text{ or } \overrightarrow{MA} = -\mathbf{a} \text{ or}$ $\overrightarrow{BN} = \frac{2}{5} \overrightarrow{BC} \text{ or } \overrightarrow{CN} = -\frac{3}{5} \overrightarrow{BC}$	M1	Oe
	a + $\frac{3}{5}(-2\mathbf{a} + 3\mathbf{b})$ or - a + 3 b + $\frac{2}{5}(2\mathbf{a} - 3\mathbf{b})$	M1	oe
	$-\frac{1}{5}a + \frac{9}{5}b$	A1	oe eg $-0.2\mathbf{a} + 1.8\mathbf{b}$ or $\frac{1}{5}(9\mathbf{b} - \mathbf{a})$ Must collect terms
25(b)	\rightarrow \rightarrow \rightarrow <i>MN</i> is not a multiple of <i>AB</i>	B1ft	ое



Q	Answer	Mark	Comments
26(2)	$-\frac{1}{2}$ or -0.5	B1	
26(a)	$-\frac{25}{64}$ or -0.390625	B1ft	ft their $-\frac{1}{2}$
26(b)	-0.381966	B1ft	ft their $-\frac{25}{64}$

 $y = -x^2 + 5x - 2$

B1

	Alternative method 1		
28	y = 2x or $(x, 2x)$	M1	oe
	$x^{2} + (2x)^{2} = 2645$	M1	oe
	$x^2 = 2645 \div 5$ or $x^2 = 529$ or $x = 23$	M1	
	(23, 46)	A1	
	Alternative method 2		
	$\frac{1}{2}y = x$ or $(\frac{1}{2}y, y)$	M1	oe
	$\left(\frac{1}{2}y\right)^2 + y^2 = 2645$	M1	oe
	$y^2 = 2645 \div \frac{5}{4}$ or $y^2 = 2116$ or y = 46	M1	
	(23, 46)	A1	



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