# GCSE MATHEMATICS 

New Specimen Papers published June 2015
Paper 2 Higher - Mark Scheme

Version 1.0

Principal Examiners have prepared these mark schemes for specimen papers. These mark schemes have not, therefore, been through the normal process of standardising that would take place for live papers.

Further copies of this Mark Scheme are available from aqa.org.uk

## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

| M | Method marks are awarded for a correct method which could <br> lead to a correct answer. |
| :--- | :--- |
| A | Accuracy marks are awarded when following on from a correct <br> method. It is not necessary to always see the method. This can <br> be implied. |
| B | Marks awarded independent of method. |
| ft | Follow through marks. Marks awarded for correct working <br> following a mistake in an earlier step. |
| SC | Special case. Marks awarded within the scheme for a common <br> misinterpretation which has some mathematical worth. |
| M dep method mark dependent on a previous method mark being |  |
| awarded. |  |

## Examiners should consistently apply the following principles

## Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

## Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

## Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

## Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

## Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

## Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

## Work not replaced

Erased or crossed out work that is still legible should be marked.

## Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

## Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

## AQA

| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| 1 | $\begin{array}{llll}1 & 2 & 4 & 8\end{array}$ | B1 |  |
|  |  |  |  |
| 2 | AAA | B1 |  |
|  |  |  |  |
| 3 | $a+20 a^{2}$ | B1 |  |
|  |  |  |  |
| 4 | $y=5 x+2$ | B1 |  |
|  |  |  |  |
|  | $\frac{4}{5}$ or $80 \%$ seen or used | M1 | oe May be implied |
| 5 | $29.4(0) \times 5 \div 4 \text { or } 147 \div 4$ <br> or $29.4(0) \div 4(\times 5) \text { or } 7.35(\times 5)$ <br> or $29.4(0) \div 0.8$ | M1 | oe |
|  | 36.75 | A1 |  |


| $\mathbf{6 ( a )}$ |  |  | B2 Any 2 or 3 of the 4 sections correct <br> B1 Any 1 of the 4 sections correct |  |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{6 ( b )}$ | $\frac{1}{12}$ |  |  |  |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 7(a) | Two of $\frac{6}{50} \quad \frac{28}{100} \frac{34}{150}$ | B2 | B1 One of $\frac{6}{50} \frac{28}{100} \frac{34}{150}$ with at most |
| :---: | :--- | :---: | :---: |
| one incorrect answer |  |  |  |


| $\mathbf{8}$ | Draws $3 x+2 y=6$ | B2 | B1 Works out or plots at least two points <br> satisfying $3 x+2 y=6$ <br> eg $(2,0)$ and $(0,3)$ |
| :---: | :--- | :---: | :--- |
|  | $x=2.5$ and $y=-0.7$ | B1ft | ft their graph <br> $\pm \frac{1}{2}$ square |


| 9(a) | Correct product using at least one prime factor | M1 | For example $2(\times) 126$ or $3(\times) 84$ or $7(\times) 36$ or $2(\times) 2(\times) 63$ or $2(\times) 3(\times) 42$ <br> May be implied eg in a factor tree or repeated division |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 2 \times 2 \times 3 \times 3 \times 7 \text { or } \\ & 2^{2} \times 3^{2} \times 7 \end{aligned}$ | A1 |  |
| 9(b) | 84 | B1 |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 10 | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | 2 parts $\rightarrow 116$ | M1 | oe |
|  | $116 \div 2 \times 16$ | M1 | oe |
|  | 928 | A1 |  |
|  | Alternative method 2 |  |  |
|  | Writes at least 3 ratios or numbers of boys and girls equivalent to $9: 7$ | M1 | eg 18:14 and 180:140 and $360: 280$ |
|  | 522 and 406 | M1 |  |
|  | 928 | A1 |  |


| 11 | $(x-4)(x+8)=0$ | B1 |  |
| :--- | :--- | :--- | :--- |


| 12 | $1.7 \times 10^{6}$ or $2 \times 10^{6}$ | B3 | B2 $1.72(8) \times 10^{6}$ or $1.73 \times 10^{6}$ or <br> 1700000 or 2000000 <br> B1 1728000 or 1730000 |
| :--- | :--- | :--- | :--- |


| 13 | $125: 27$ | B1 |  |
| :---: | :---: | :---: | :--- |


| Q Answer | Mark | Comments |
| :--- | :--- | :--- | :--- |


| 14(a) | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | $10 \div 4 \text { or } 2.5$ <br> or $4 \div 10$ or 0.4 <br> or $\frac{1}{2} \times(18+10) \times 25$ or 350 | M1 | oe |
|  | $18 \div$ their 2.5 <br> or $18 \times$ their 0.4 or 7.2 <br> or $25 \div$ their 2.5 <br> or $25 \times$ their 0.4 or 10 | M1dep | oe |
|  | $\frac{1}{2} \times(18+10) \times 25 \text { or } 350$ <br> and $\frac{1}{2} \times($ their $7.2+4) \times$ their 10 or 56 | M1dep | Must see working |
|  | $350-56=294$ | A1 | Do not award without working seen |
|  | Alternative method 2 |  |  |
|  | $10 \div 4 \text { or } 2.5$ <br> or $4 \div 10$ or 0.4 <br> or $\frac{1}{2} \times(18+10) \times 25$ or 350 | M1 | oe |
|  | $($ Area scale factor $=)(\text { their } 2.5)^{2}$ or (their 0.4) ${ }^{2}$ | M1dep |  |
|  | their $350 \div(\text { their } 2.5)^{2}$ <br> or their $350 \times(\text { their } 0.4)^{2}$ or 56 | M1dep | Must see working |
|  | $350-56=294$ | A1 | Do not award without working seen |
| 14(b) | $\frac{18-10}{2}$ or 4 | B1 |  |
|  | $\tan x=\frac{25}{\text { their } 4}$ | M1 |  |
|  | [80.9, 81] | A1 |  |


| Q Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 15 | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | 1800 | B3 | B2 $a \times b \times c \times d$ with at least 3 correct from 9, 10, 10 and 2 <br> B1 $\mathrm{a} \times \mathrm{b} \times \mathrm{c} \times \mathrm{d}$ with at least 2 correct from 9, 10, 10 and 2 <br> or identifies 9 possibilities for first digit or identifies 2 possibilities for final digit |
|  | Alternative method 2 |  |  |
|  | 9000 | M1 | The number of digits between 1000 and 9999 inclusive |
|  | their $9000 \div 5$ | M1dep |  |
|  | 1800 | A1 |  |


| $\mathbf{1 6}$ | $6 c\left(c^{2}+5\right)$ or $3\left(c^{2}+5\right)$ | M1 |  |
| :--- | :--- | :--- | :--- |
|  | $\frac{6 c\left(c^{2}+5\right)}{3\left(c^{2}+5\right)}$ | M1 | This mark implies first M1 |
|  | $2 c$ and multiple of 2 so even | A1 | oe statement <br> Must see method |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 17(a) | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 93000000 \times 2 \pi \\ & \text { or } 186000000 \pi \\ & \text { or }[584000000,584412000] \end{aligned}$ | M1 | oe <br> Allow working in millions |
|  | $\begin{aligned} & 365 \times 24 \\ & \text { or } 8760 \end{aligned}$ | M1 |  |
|  | their $186000000 \pi \div$ their 8760 | M1 | oe Allow working in millions Only allow if first M1 gained or if their circumference is $93000000 \times \pi$ |
|  | $\left[6.6 \times 10^{4}, 6.7 \times 10^{4}\right]$ | A1 | oe |
|  | Alternative method 2 |  |  |
|  | $\begin{aligned} & 93000000 \times 2 \pi \\ & \text { or } 186000000 \pi \\ & \text { or }[584000000,584412000] \end{aligned}$ | M1 | oe Allow working in millions |
|  | their $186000000 \pi \div 365$ or [1 598 904, 1600 033] | M1 | oe <br> Allow working in millions <br> Only allow if M1 gained or if their circumference is $93000000 \times \pi$ their 365.25 can be $365.25 \times 24$ or $365.25 \times 60$ |
|  | their $\left[1.6 \times 10^{6}, 1.602 \times 10^{6}\right] \div 24$ | M1 |  |
|  | $\left[6.6 \times 10^{4}, 6.7 \times 10^{4}\right]$ | A1 | oe |
| 17(b) | The average speed would be (slightly) lower | B1 | oe |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 18(a) | $(n-6)^{2}$ could be zero (so she is <br> wrong) <br> or <br> The sixth term is 1 | B1 | oe |
| :--- | :--- | :--- | :--- |
| 18(b) | 1 | B1 |  |

19
$\frac{x}{3}$
B1

| 20 | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | $2=k \sqrt{36}$ or $\sqrt{36}=6$ | M1 |  |
|  | $(k=) 2 \div$ their 6 or $\frac{1}{3}$ | M1dep |  |
|  | $5 \div$ their $\frac{1}{3}$ or $15(\sqrt{a}=)$ | M1 | oe |
|  | 225 | A1 |  |
|  | Alternative method 2 |  |  |
|  | $2 k=\sqrt{36}$ or $\sqrt{36}=6$ | M1 |  |
|  | ( $k=$ ) their $6 \div 2$ or 3 | M1dep |  |
|  | $5 \times$ their 3 or $15(\sqrt{a}=)$ | M1 | oe |
|  | 225 | A1 |  |
|  | Alternative method 3 |  |  |
|  | $2 k=\sqrt{36}$ or $\sqrt{36}=6$ | M1 |  |
|  | $5 \div 2$ or 2.5 | M1 |  |
|  | their $6 \times$ their 2.5 or $15(\sqrt{a}=)$ | M1dep | dep on M1 M1 |
|  | 225 | A1 |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |

## Alternative method 1

| 1.2 or 0.85 | M 1 |  |
| :--- | :---: | :--- |
| $1 \div 0.85$ or $1.1(7 \ldots)$ or 1.18 | M 1 |  |
| $1.1(7 \ldots)$ or 1.18 and 1.2 and <br> (Option) A | A 1 |  |

## Alternative method 2

| 1.2 or 0.85 | M1 |  |
| :--- | :---: | :--- |
| $1 \div 1.2$ or $0.83(\ldots)$ | M1 |  |
| $0.83(\ldots)$ and 0.85 and <br> (Option) A | A1 |  |

Alternative method 3

21

| $450 \times 1.2$ or 540 <br> or <br> $x \times 0.85$ or $0.85 x$ | M1 | $x$ is the usual cost of the box and may be a <br> numerical value |
| :--- | :---: | :--- |
| $x \div$ their 540 or their $0.85 x \div 450$ | M1dep |  |
| $0.00185(\ldots) x$ and $0.00188(\ldots) x$ <br> and (Option) A | A1 | oe |

## Alternative method 4

| $450 \times 1.2$ or 540 <br> or <br> $x \times 0.85$ or $0.85 x$ | M1 | $x$ is the usual cost of the box and may be a <br> numerical value |
| :--- | :---: | :--- |
| their $540 \div x$ or $450 \div$ their $0.85 x$ | M1dep |  |
| $\frac{540}{x}$ and $\frac{529 .(\ldots)}{x}$ and | A1 | oe |
| $($ Option) A |  |  |

## Alternative method 5 on next page

| Q Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 21 | Alternative method 5 |  |  |
| :---: | :---: | :---: | :---: |
|  | $\frac{1}{6}$ (free for A ) | M1 | oe fraction or decimal or percentage |
|  | $\frac{3}{18}\left(\right.$ free for $A$ ) and $\frac{3}{20}$ (free for $B$ ) | M1 | oe pairs of fractions or pairs of decimal or pairs of percentages |
|  | $\frac{3}{18}$ (free for $A$ ) and $\frac{3}{20}$ (free for $B$ ) and (Option) A | A1 |  |



| Q Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 22 | Alternative method 4 |  |  |
| :---: | :---: | :---: | :---: |
|  | $\frac{15}{25}$ or $\frac{30}{11}$ | M1 |  |
|  | $\frac{15}{25} \times \frac{30}{11}$ or $\frac{18}{11}$ | M1dep | oe fraction |
|  | their $\frac{18}{11} \times 22$ | M1 |  |
|  | 36 | A1 |  |
|  | Alternative method 5 |  |  |
|  | $25 \times h=22$ or $\frac{22}{25}$ or 0.88 | M1 | oe |
|  | $0.88 \div 11$ or 0.08 | M1dep | oe eg frequency density axis labelled with correct scale |
|  | their $0.08 \times 30 \times 15$ | M1 |  |
|  | 36 | A1 |  |


| 23 | $\frac{1}{2} \times \frac{4}{3} \times \pi \times 6^{3}$ or $144 \pi$ | M1 | oe eg [452, 452.45] |
| :---: | :---: | :---: | :---: |
|  | $\frac{2}{5} \times \text { their } 144 \pi=\frac{1}{3} \times \pi \times x^{2} \times 12$ <br> or $57.6 \pi=4 \pi x^{2}$ | M1 | oe eg $[180.8,181]=[12.5,12.6] x^{2}$ <br> Must equate two volumes in terms of $\pi$ |
|  | $3 \times \frac{2}{5} \times$ their $144 \pi \div 12 \pi$ or 14.4 | M1dep | oe eg their $[180.8,181] \div$ their $[12.5,12.6]$ dep on 2nd M1 <br> Correct working to isolate $x^{2}$ |
|  | [3.79, 3.8] | A1 |  |


| Q Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 24(a) | $\cos x=\frac{O A}{15} \text { or } O A=15 \cos x$ | M1 |  |
| :---: | :---: | :---: | :---: |
|  | $O A=15 \cos x$ <br> and $O B=15+2$ <br> and $h=O B-O A=17-15 \cos x$ | A1 |  |
| 24(b) | $\begin{aligned} & 17-15 \cos 120 \\ & \text { or } \\ & 15 \sin 30 \text { or } 7.5 \end{aligned}$ | M1 |  |
|  | 24.5 | A1 | oe |
| 24(c) | $(180,32)$ | B2 | B1 one correct coordinate $\text { SC1 }(32,180)$ |


| 25(a) | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & a=2 \text { or } 2\left(x^{2}-3 x+2.5\right) \text { or } \\ & 2\left(x^{2}-3 x\right)+5 \end{aligned}$ | M1 |  |
|  | $x^{2}-3 x=(x-1.5)^{2}-1.5^{2}$ | M1dep | oe <br> ft their $x^{2}-3 x$ |
|  | $a=2$ and $b=1.5$ and $c=0.5$ | A1 | oe eg $2(x-1.5)^{2}+0.5$ |
|  | Alternative method 2 |  |  |
|  | $a=2$ | B1 |  |
|  | $\begin{array}{ll} x^{2}-b x-b x+b^{2} & \text { or } \\ x^{2}-2 b x+b^{2} & \text { or } \\ -2 a b=-6 & \text { or } \\ -a b=-3 & \text { or } \\ b=1.5 & \end{array}$ | M1 | oe |
|  | $a=2$ and $b=1.5$ and $c=0.5$ | A1 | oe eg $2(x-1.5)^{2}+0.5$ |


| Q Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 25(b) | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | their $2(x-1.5)^{2}=8.5-$ their 0.5 | M1 |  |
|  | their $(x-1.5)= \pm \sqrt{\frac{8.5-\text { their } 0.5}{2}}$ | M1dep | oe |
|  | 3.5 and -0.5 | A1 | oe |
|  | Alternative method 2 |  |  |
|  | $\begin{aligned} & 2 x^{2}-6 x-3.5(=0) \text { or } \\ & 4 x^{2}-12 x-7(=0) \end{aligned}$ | M1 | oe 3-term quadratic equation or expression |
|  | Correct use of quadratic formula eg $\frac{--12 \pm \sqrt{(-12)^{2}-4 \times 4 \times-7}}{2 \times 4}$ or correct factorisation eg $(2 x-7)(2 x+1)=0$ | M1dep | oe |
|  | 3.5 and -0.5 | A1 | oe |


| $\mathbf{2} \mathbf{2 6}$ | $144 \%$ or 1.44 seen | B1 |  |
| :---: | :--- | :---: | :--- |
|  | $\sqrt{1.44}$ or 1.2 | M1 | oe |
|  | their $1.2 \times 32$ | M1dep |  |
|  | 38.4 | A1 |  |

